Fifth entry: should read ‘2 π/3 Once’ (not ‘Twice’).
A new (eighth) entry: K₁ = 0, K₂ = -1, Region θ = π/2 Once.
2) Section 2.5.1, prgh.2, line 15, pg.864.
Little Σ should be squared.
3) pg.870.
First equation at top left of page: should read
\[ ci + \text{binary code}(\text{ec})/(2^e2^w) \equiv c_F \]
An asterisk should appear in the caption for Fig.14 preceding ‘See TMS ...
4) Section 4.1.2, prgh.1, pg.872.
Delete lines 21 through 24; i.e. delete, ‘worsens when... ...problem’
5) pg.874.
The approximation to h(n) equation should take the absolute value on the left hand side.
6) Section 1.2.2, last paragraph, line 11, pg.858; should read: ‘gain and less. The responsibility...’

PART II - FIR

THE IMPLEMENTATION OF A ONE-STAGE MULTI-RATE 64:1 FIR

DECIMATOR FOR USE IN ONE-BIT SIGMA-Delta A/D APPLICATIONS

JON DATTORRO, ALBERT CHARPENTIER, & DAVID ANDREAS

ENSONIQ Corporation

II-0 INTRODUCTION

Sigma-Delta modulation is emerging as a preferred alternative to successive approximation techniques for analog to digital conversion [42]-[53]. The Sigma-Delta system can, conceptually, be divided into two distinct parts: the analog front end (the one-bit modulator), and the digital decimation filter. The decimation filter outputs the desired digital signal. This paper concerns itself with the implementation of the decimation filter only, when presented with a one-bit stream from the front end flash converter (a lone comparator). The advantages of the binary state signal are capitalized on in this design.

The attraction to Sigma-Delta A/D converters in terms of hardware, is the relaxed constraints on the input anti-alias filter and the lack of the need for a sample/hold circuit. The foremost theoretical reason for the preference of Sigma-Delta is the fact that [51] as the signal level goes down, the harmonic distortion increases at a much slower rate. This is primarily due to the superb linearity of the analog front end. In the one-bit case, the linearity easily exceeds that of the best successive approximation designs.

The Sigma-Delta process, in simple terms, spreads the quantization noise of a very low resolution flash A/D converter over a broad region covering several Megahertz, and then shapes that noise via feedback of filtered quantized signal. The output of the low resolution A/D converter is presented to the decimation filter whose task it is to take the low resolution high speed samples and convert them to high resolution low speed samples.

II-1 THEORY

II-1.0 DECIMATION

Our one-bit A/D converter is running at 3.072 MHz. The desired sample rate is 48kHz. We then have a decimation ratio of 64. If we use an FIR filter to perform the decimation, then the current decimator output is not dependent on previous outputs because of the nonrecursive structure. There is, therefore, no filter output truncation noise recirculation to worry about. In the time domain we are allowed to literally throw away 63 out of every 64 output samples calculated. In fact, it is not even necessary to calculate those 63 intermediate samples. If we use only one FIR filter to perform the decimation from the 3.072MHz rate to the 48kHz rate, then we say that we are decimating in one stage.

Other commercial implementations [44] [47] [50] [51] of the decimator comprise several small moving average type FIR stages in cascade, operating at a much higher rate. This is a good approach but the attraction to the one-stage approach is the small area of silicon upon which a large ROM can be constructed (ROM is cheap), and the high alias rejection at the first foldover frequency (-110dB at 28kHz for a 48kHz sample rate). We have found that 2048 22-bit coefficients are required at 3 MHz to reach the theoretical performance level of a 16 bit A/D converter, which agrees with Adams’[47] assessment of about 4000 coefficients at 6MHz.

Figure 18 shows the process of decimation in the frequency domain. In Figure 18(a) a fictitious baseband audio spectrum is shown out to 3.072MHz with its first replication. The prime on the frequency argument denotes the high sample rate. Figure 18(b) shows the FIR transfer. The original spectrum is multiplied by the FIR transfer at the high sample rate (not shown) corresponding to the convolution in the time domain. Note that while the stopband attenuation of the FIR is high, it is not absolute zero. We can infer that the quality of the decimation is somehow related to the absolute spectral level of that out-of-band (the 24kHz -> 3MHz region) material and the degree to which it becomes attenuated. This is true, since when we throw away 63 out of 64 samples, the spectrum in Figure 18(c) results which shows aliasing as a result of the decimation. The aliases are shifted replications of the filtered 3.072MHz spectrum. We need to know the total accumulation of unwanted alias distortion. First note some incidentals concerning the aliases: 1) there are only 63 aliases into the audio baseband [40], 2) the baseband spectrum remains symmetrical after decimation.
II-1.1 DECIMATOR ALIAS NOISE

To determine the amount of alias distortion, we need to know whether the output of band signal is correlated or uncorrelated to the base band audio signal. If the out of band signal were correlated with the audio signal, the amount of aliasing noise in power spectral level could be as bad as 10log(63Sx) [22,chap.3-4], or 36dB over Sy, where Sy is the power spectral density of the FIR filtered out-of-band signal prior to decimation. Refer to Figure 19. It becomes the job of the Sigma-Delta analog front end to make sure that the out of band signal is uncorrelated. In this case the amount of aliasing noise is approximately 10log(63Sy), or 18dB over Sx. This alias noise, 63Sy, is combined as the sum of the squares with the in-band pre-decimation noise power spectral density, Sx, to get the total post-decimation noise power spectral density in-band,

\[ S_y = S_x + 63S_x. \]  

To reach the noise performance of a 16 bit converter, we need at least 90dB S/N in the 24kHz baseband. The noise power, N, refers to the integral of the total noise power spectral density, Sx. In the time domain, this means that the RMS level of the noise is such that only the LSB would ever be toggled in response to the noise alone. In the frequency domain it means that the power spectral density, SY, should have a level of about -140dB [22,chap.6-2] with respect to a unity level sinusoid. Refer to Figure 20. The total noise power can be estimated in the frequency domain over a 24kHz bandwidth as follows:

\[ 10\log(N) = 10\log(\int_0^{24kHz} S_y \, df) = 96\text{dB} \]  

\[ \text{when } S_y = 10^{-140/10} \text{[V}^2/\text{Hz]} \]

We can now determine the required FIR attenuation. Referring to Figure 19, using (II-1) and realizing that

\[ S_x = 10^{(M+H_p)/10} \text{[V}^2/\text{Hz]} \]

then,

\[ \frac{1}{H_p} \equiv 10\log(S_y/S_x) = 18-M[\text{dB}] \]  

for \( S_q < S_y \)

where M is the level of the out-of-band pre-decimation modulator noise power spectral density in dB (about -34dB, [44, Figure 21]), and \( H_p \) is the (negative) FIR stopband attenuation level in dB. When the noise contribution due to aliasing is only 18dB, and 10log(Sy) is about -144dB, then we find from (II-3) that the required FIR stopband level, H_p, is about -126dB.

Figure 21 shows a simulated modulator output signal and noise floor in response to an input sinusoid. The simulation was performed in floating point arithmetic. The out-of-band noise power spectral density, M, is lower than our conservative estimate of -34dB, above. The bandwidth of this plot is 1.536MHz and so the signal, at exactly 1.500kHz, is scrunched up against the left hand side. Figure 22 shows the audio band only, of the same modulator output. The in-band noise power spectral density, S_q, is a little higher than we would like but this is compensated in equation (II-3) by the lower out-of-band noise. Figure 23(a) shows the audio band of the simulated decimator output, post-decimation, in response to the modulator output of Figure 21. This part of the simulation was performed using all integer arithmetic. Figure 23(a) represents a 21 bit decimator output. Figure 23(b) represents a 16 bit decimator output. The character (or correlation) of the noise floor after truncation to 16 bits depends totally on the modulator design which can be considered to be a pre-dithered noise shaping system. Harmonic distortion is more likely here because the 1-bit sinusoid frequency is a sub-multiple of 48kHz.

Figures 21, 22, and 23 are estimates of power spectral density [4,chap.11]. The size of the FFT required for adequate spectral resolution was 65536 points. Although our plots of (power) spectral density use decibels on the ordinate, they should not be confused with “noise power” which is the integral of spectral density.

II-1.2 DECIMATOR FILTER SHAPE

To get 126dB of attenuation requires at least 21 bits (assuming 6dB per bit) of resolution in the FIR coefficients. We can understand this intuitively by realizing that the FIR filter coefficients are quantized samples of the impulse response of the desired filter. If the quantization RMS noise floor of the coefficients exceeds the desired stopband level, then it is not likely that the filter will meet specifications. For example, in order that a one-bit signal be attenuated downward 21 bits, the mathematics at the 21 bit level must be accurate. Obviously, the greater the precision in the calculations, the more this will be true. The noise floor at 21 bits, then, is the lower bound, while some number of bits in excess of 21 becomes the upper bound on the number-of-bit criterion for accurate high attenuation filtering.

Another way to look at this is in analogy to IIR filters. Recall that the coefficient resolution of an IIR filter primarily determines deviation from the shape of the desired filter; the same is true for FIR. This can be seen easily by taking the Fourier transform of the digital impulse response.

In reality, the 21 bit impulse response does not utilize the whole quantization space and we can lose as much as about 4.4 dB from the theoretical limit. For this reason we will use 22 bit coefficients to guarantee 126dB attenuation. The 2048 quantized coefficients which comprise the FIR decimator are shown in Figure 24. The coefficients were calculated on a VAX8700 at ENSONIQ using a standard Parks/McClellan algorithm in quadruple precision, and about 1 hour of CPU time. The FIR transfer function is shown in Figure 25; it was calculated using an FFT on the 22 bit coefficients. Note that the normalized passband width is only 0.0064 which yields a -3dB point at 22kHz, and the attenuation is 110dB at 28kHz. The transition region is therefore about 392dB.
per octave. A blowup of the passband is shown in Figure 26; the ripple is negligible.

11.3 FIR COEFFICIENT GAIN AND OFFSET

The floating point coefficients out of the Parks/McClellan algorithm are all much less than 1.0 in magnitude; interestingly enough, the algorithm produces a unity gain design which means that the gain is unity in the passband. This means that we can introduce a gain into the passband if we desire to compensate some system loss and/or to eliminate leading binary zeroes from the coefficients to increase their precision. If the minimum floating point value produced by the Parks/McClellan algorithm is called \( \text{min} \) (-0.00312), and the maximum value is called \( \text{max} \) (0.0148), then the maximum gain, \( g \), that we could ever introduce while still maintaining 22 bit precision is

\[
g \leq 1/(\text{max}-\text{min}) \approx 55.7
\]  \( \text{(II-4a)} \)

In our implementation we work with unsigned coefficients to simplify the hardware. In this case we need to add an offset,

\[
d \geq \text{min}
\]  \( \text{(II-4b)} \)

to the floating point coefficients prior to introducing the gain factor so as to make all the floating point coefficients positive and to maximize the utilized quantization space.

The normalized impulse response is then,

\[
h_{\text{norm}}(n) = \{ h(n) + d \} g
\]  \( \text{(II-4c)} \)

where \( h(n) \) are the floating point coefficients produced by the design procedure, \( d \) is the floating point offset, and \( g \) is the floating point gain factor. The floating point coefficients, \( h_{\text{norm}}(n) \), are all non-negative as a result of the offset. They will later be encoded and then stored in ROM using 22 bits of precision but having no sign bit.

The desired (standard) floating point convolution is,

\[
y(n) = \sum h(k)x(n-k)
\]  \( \text{(II-5)} \)

The calculation we will actually perform on chip is,

\[
y(n) = \left\lfloor \left( \sum (h_{\text{norm}}(k)x_{\text{norm}}(n-k)+C_0[1-x_{\text{norm}}(n-k)]) \right) - g/2 \right\rfloor
\]  \( \text{(II-6)} \)

where, \( x_{\text{norm}}(n-k) = 1 \) or \( 0 = x(n) + 0.5 \)

Since the quantized signal, \( x_{\text{norm}}(n) \), has only two states, we can force no symmetry about zero. It has, therefore, a DC offset of 0.5 which should be subtracted out of the accumulation. This is the purpose of \( g \) which is subtracted after the completion of the accumulation. The second term in equation (II-6) involving \( C_0 \) will neutralize the term, \( dg \), in the normalized coefficients in (II-4c). \( C_0 \) is the floating point representation of a positive constant whose value is chosen such that \( N (=2048) \) times \( C_0 \) exceeds the available accumulator dynamic range; i.e., in floating point,

\[
NC_0 = (NI/2^{22}) > g
\]  \( \text{(II-7)} \)

for a trivial binary integer (a binary integer having only one nonzero digit). The purpose of \( C_0 \) will be to trivially overflow the accumulator into another modulo but always into the same place within the same modulo.

Expanding equation (II-6) we find,

\[
y(n) = \sum \{ [gh(n) + dg][x(n-k) + 0.5] + C_0[1 - (x(n-k) + 0.5)] \}
\] \( - g/2 \)

(II-8a)

\[
= 0.5g \sum \{ h(n) \} - g/2
\] \( + \sum \{ gh(n)x(n-k) + 0.5dg + 0.5C_0 + [dg - C_0]x(n-k) \} \) (II-8b)

The first two terms vanish because the Parks/McClellan filter design is unity gain (the coefficient quantization produces a tiny DC offset). We can only rid the last term if

\[
C_0 = dg
\]  \( \text{(II-8c)} \)

At this point we need to adjust \( d \) and \( g \) so that their product equals \( C_0 \) exactly, for \( C_0 \) constrained as in (II-7). If we do this, then (II-8b) becomes,

\[
y(n) = g \sum \{ h(n)x(n-k) \} + NC_0
\]  \( \text{(II-9)} \)

Note that the multiplication of two trivial binary integers results in another trivial binary integer. Since \( NC_0 \) has been chosen to overflow the accumulator such that if the \( x_{\text{norm}}(n-k) \) were all zero then the accumulator would be zero, then, in effect, \( NC_0 \) goes away and we are left with the desired convolution times a gain factor.

11.4 FIR ACCUMULATOR WIDTH

The accumulator size is not arbitrary; it must be chosen such that we know which bits out of the accumulator will be used as the output bits. Since the normalized filter uses unsigned Q22 coefficients having widths of 22 bits, and the Q0 signal is one-bit, then at least a 22-bit accumulator is required, following the rule: \( \text{Q22Q0} = \text{Q22, 22-bit} \times 1\text{-bit} = 23\text{-1 redundant} \) (in this case, superfluous) sign bit = 22 bits.

If the gain, \( g \), in (II-4c) were equal to 1, then a 22 bit accumulator would be sufficient because the filter design is unity gain. But, since the maximum allowable value of \( g \), which will not demand greater than 22-bit coefficient precision, is 55.7 for our particular filter design (I-4a), we choose \( g \) to be \( 2^5 (=32) \). This particular value of filter gain, \( g \), serves to eliminate 5 leading binary zeroes from the coefficients, \( h(n) \), and establishes the number of extra bits required in the accumulator to be exactly 5, which brings us
up to 27 bits. If there were a system loss to compensate, we could use a $g$ of greater value (but less than 55.7), having no need to adjust the accumulator width.

Finally, we want one more (guard) bit in the accumulator which we will use for overflow detection. (The proper way to detect overflow is discussed in [39, Appendix 2] and in section I-3.1 here.) This brings us to the requirement of a 28 bit accumulator. The accumulator output comprises the MSBs excepting the guard bit.

II-1.4.1 BOOKKEEPING

Even though all the normalized coefficients were non-negative, equation (II-9) indicates that the result, $y(n)$, is a signed quantity because both $h(n)$ and $x(n)$ are signed. After we account for the gain, $g$, the effective binary point in the accumulator stays between the guard bit and the 27th bit (calling the LSB the first bit). Since $x(n)$ is bounded in magnitude by 0.5, and since the filter design was unity gain, then $y(n)$ must obey the same bound. This is the purpose of the $-g/2$ term in equations (II-6) and (II-8). Specifically,

$$-0.5 \leq y(n)/g < 0.5$$

We can now move the binary point one place right, effectively multiplying by two, recovering the sign bit. The 28 bit accumulator ends up in Q26 format.

II-1.5 SPECIFIC VALUES OF FIR COEFFICIENT GAIN AND OFFSET

The present section is tedious and can be skipped without any loss of comprehension. It is included for the engineer who wishes to pursue this design philosophy.

Equation (II-4a) expresses the maximum value of the filter gain, $g$, which occurs for a coefficient offset, $d = -\text{min}$. In general, to insure normalized coefficients bounded by 1, we can derive the following bounds on $C_0$:

$$g \leq 1/(\text{max} + d) \quad (\text{II}-10)$$

Using this equation, (II-8c), and tightening the bound in (II-7) to account for the extra accumulator (guard) bit, we can derive the following bounds on $C_0$:

$$2^{W/2}2^{2N} \leq C_0 \leq 1 - g(\text{max}) \quad (\equiv 0.526)$$

(II-11a)

where $W$ is the accumulator width, 22 is the desired coefficient resolution, and $N$ is the number of coefficients.

For this particular implementation having a gain chosen to be 32, and our filter impulse response which, non-normalized, has a max of about 0.0148 and a min of about -0.00312, the only possible values of $C_0$ are (in floating point):

$$C_0 = dg = 2^{1/2}2^{2N}; \text{ for } i = W, W+1, W+2, W+3, W+4 = 0.03125, 0.0625, 0.125, 0.25, 0.5; \text{ or } 2^{0.4} g$$

Actually, $C_0$ can be the sum of any subset of these values and still cause the accumulator to overflow trivially, as long as (II-11a) is satisfied. But there is another constraint on our choice of $C_0$ which raises the lower bound on the subset sum. Whereas (II-10) insures normalized coefficients, the inequality (II-4b) insures that the coefficients are all positive. From (II-4b) we can derive,

$$(0.0998 \approx (-\text{min})g \leq C_0 \quad (\text{II}-11b)$$

We will set $C_0$ as close as possible to $-\text{min}/(\text{max}-\text{min})$ (-0.174) to maximize the conceivable range of $g$ in (II-11);

$$C_0 = 0.0625 + 0.125 = 2^{-4} + 2^{-3} = 0.1875$$

In general, choosing $g$ any higher than $2^5$ would require another accumulator bit. If there were a system loss to compensate however, $g$ can be chosen to exceed $2^5$, and then $C_0$ can be set according to (II-11) without the need for an extra accumulator bit. $g$ is not constrained to be an integer. As long as (II-11) is complied, the coefficient offset, $d$, will effectively adjust itself, however $g$ is adjusted, to satisfy (II-8c).

In summary the Parks/McClellan floating point coefficients would be encoded in (unsigned) binary for storage in ROM using the following equation:

$$\text{binary code}(h_{\text{norm}}(n)) = 2^{2W}(gh(n) + C_0)$$

As a final note, to simplify the hardware, the term $g/2$ in equation (II-6) could be integrated into $C_0$ and the coefficients, $h_{\text{norm}}(k)$, which would eliminate the final subtracter circuit. This affects the preceding math which can be re-figured using $d' = d-1/2N$ in place of $d$, and $C_0' = C_0 - g/2N = d'g$ in place of $C_0$. $C_0$ would still have the lower bound in (II-11a).

II-2 HARDWARE

II-2.0 BRUTE FORCE IMPLEMENTATION

The speed requirements of a brute force implementation would be excessive for low power CMOS. Since the input signal is one bit in width, we are performing only conditional additions; no multiplications. At a 48kHz output rate, the accumulation time would be 20.83μS / 2048 coefficients = 10μS. This is about an order of magnitude too fast. The decimation rate is 64. This means that every 64-3.072MHz clocks, we must output a new sample. If we use the 3MHz system clock as the accumulator clock, then we could only calculate one 64-tap FIR at the 48kHz rate.

To solve this problem, we will use 32 parallel processes all operating at the system rate of 3MHz [41][54]. Each parallel process, operating using a time skew of 64 clocks with respect to its neighbor, will only be required to output a sample every 2048 system clocks. Not more than one parallel process will yield an output at any given time. In this manner, a sample will be output every 64-3MHz clocks from a successive parallel process. Although the output rate will be 48kHz, each one of the
parallel processes will be operating at an subsampled output rate of only 1.500kHz.

Formally, the structure we have described is called a "multirate filter" [40] because the final output rate is not the same as any one parallel process' output rate. The structure is shown in Figure 27. We will omit the Co offset compensation for clarity. The parallel processes are themselves FIR filters working at a 1.5kHz rate. It is interesting that the output of each of these slow FIRs can be combined to form the desired output, \( y_{des}(n) \), with no aliasing due to 1.5kHz replications. The time skew adds a phase factor to the transfer of each of the multirate FIRs so that their sum produces the desired result. It is also interesting to note that the impulse response of the decimator at the 48kHz rate is time-variant; there are 64 different impulse responses.

II-2.1.1 CONCEPT - MULTIRATE PROCESS

This section is theoretical and can be skipped without loss of continuity.

The commutator in Figure 27 is the processing element that makes the decimator multirate. A simple time domain proof that the commutator can be used without unwanted aliasing is as follows: Assume that \( y_{des}(n) \) is the desired 48kHz rate (decimated by 64) signal which is known to be good. Then

\[
y_{des}(n) = \sum_{p=0}^{31} y_p(q) \quad ; \quad n \leq 48kHz
\]

(II-12)

where \( y_p(q) \) is the 1.5kHz rate signal (\( y_{des}(n) \) further subsampled by 32) from each parallel process; i.e.,

\[
y_p(q) = y_{des}(32q - p)
\]

(II-13)

Then there will be no unwanted aliasing only if,

\[
n = 32q - p
\]

(II-14)

For an alternate proof in the frequency domain, see [40,Sec.4.2.1]. Essentially, the proof there can be boiled down to first time-shifting the desired sequence,

\[
x_p Y_{des}(z)
\]

(II-15)

and then subsampling (decimating further) by 32,

\[
Y_p(z) = (1/32) \sum_{k=0}^{31} e^{-j(\omega - 2\pi k/32)p} Y_{des}(e^{j(\omega - 2\pi k/32)})
\]

(II-16)

Then prove that:

\[
Y_{des}(z) = \sum_{p=0}^{31} Y_p(z)
\]

(II-17)

II-2.2 MULTIPLEXING

Figure 28 is more efficient in terms of ROM since there is no longer a duplication of it. The ROM is now segmented having 32 outputs from 32 segments. Each segment holds 64 unique coefficients. The 6 LSBs from the 3MHz counter address all the ROM segments at once. Each segment runs through each of its 64 coefficients at the 3MHz rate and sends them to its respective output. The coefficient segment assignment is shown. The multiplexers now route any one of their 32 22-bit inputs to their respective output. The routing is controlled by the 5MSBs out of the counter at the 48kHz rate. The operation below the multiplexers is the same as before. The purpose of the multiplexers is to perform the coefficient rotation. Looking at multiplexer #1, we see that the segments are ordered into it
(left to right) starting with segment #1. Multiplexer #2 orders the segments such that segment #32 is in the first (leftmost) input while segment #1 is the second input. This agrees with the reasoning we used to order the coefficients in Figure 27.

II.2.3 VLSI

The actual physical organization is shown in Figure 29. There, all the multiplexers have been replaced by one barrel shifter. The multiplexer input wiring in Figure 28 was quite hairy. The barrel shifter in Figure 29 takes any one of its 32 inputs and routes it to any one of its 32 outputs. The wiring external to the barrel shifter is greatly simplified. Internally, the barrel shifter embodies a type of matrix organization. The ROM is still segmented as before, controlled by the 6 LSBs out of the counter at the 3MHz rate. The accumulators are now aligned vertically one above another to form a more compact silicon structure.

The actual VLSI realization uses a bit-wise organization such that bit 0, for example, for all the coefficients in the ROM, all the barrel shifter inputs, and for all the accumulators, are aligned in one column. This allows easy decomposition for coefficients of varying widths.

The advantages of this design include an easy stereo implementation; all that must be done is to double the number of accumulators. The ROM and barrel shifter are shared for any number of channels. The present implementation has 64 accumulators for stereo operation. Every 4 accumulators comprise one multiplexed accumulator. We estimate the dimensions at about 140 X 180 mils.

ACKNOWLEDGEMENT

We would like to thank Steve Kozachyn of ENSONIQ for the excellent job done on the figures for both this and the original 1988 November Journal publication.

REFERENCES

[21] M. Richards, “Improvements in Oversampling Ana-
Fig. 6. Unity gain design.

Fig. 8. Direct Form I having truncator.

Fig. 11. Second order error feedback.

Fig. 11-11. Second order truncation error cancellation showing all truncation errors.

Fig. 15. Showing the saturator explicitly, forced overflow analysis.

Fig. 16. Typical forced overflow response for a sinusoidal input.

Fig. 17. Stability triangle for positive topology.

Fig. 19. Relationship of $M$, $S_y$, and $H_F$ to achieve $S_y$, the in-band spectral density after decimation.
Fig. 18. Decimation in the frequency domain.

Fig. 20. Required power spectral density of noise power, $N$, to achieve 90 dB S/N.

Fig. 21.
Fig. 23A.

Frequency

Decimator output 8 b it

Fig. 23B.

Frequency

Decimator output 16 b it

Fig. 24.

Frequency

FIR coefficients

Fig. 25.

Frequency

Frequency response of decimator

Sinusoid is 1.5 kHz

\[ \text{Sin}(f) = \sin(2\pi f t) \]

But noise is still uncorrelated due to the aliasing and frequency response of \( \sin \).

This was previously discussed.

AES 7th INTERNATIONAL CONFERENCE
IMPLEMENTATION OF DIGITAL FILTERS FOR HIGH-FIDELITY AUDIO

Fig. 26.

Fig. 27. Multirate FIR decimator.
Fig. 28. ROM collapse.

Fig. 29. Physical organization — MUX collapse.