

STOMPBOX DESIGN WORKSHOP

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FX Basics: Filtering

Filtering effects modify the frequency content of the audio signal, achieving **boosting or weakening** specific **frequency bands** or regions.

Although their broad application to processing sound signals dates back from the early days of recording, their use application to processing guitar electrical signal may have started in the 1950s.

Filtering effects make use of **filters**, which are signal processors which **alter magnitude and phase** of signals by different amount s to different frequency components.

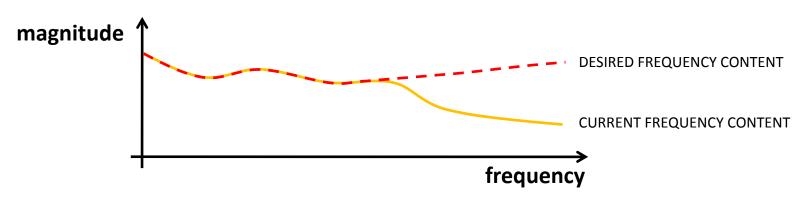
Ex: equalization, wah-wah



Equalization

Original term coined from the task of 'adjusting the balance between of (or *equalize*)' different frequency components of a signal.

Equalization is commonly achieved by means of a device specifically designed for a **user-friendly control** of the parameters governing the **behavior of filters** used for its construction.



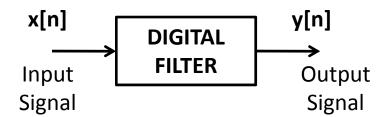
User-friendly interface to controlling filters so that a **desired alteration** is achieved...

DIGITAL FILTERS!



Digital Filters

Systems that perform mathematical operations (multiplications and additions) to a **discrete input signal** x[n] to modify some of its characteristics and **obtain a discrete output signal** y[n].

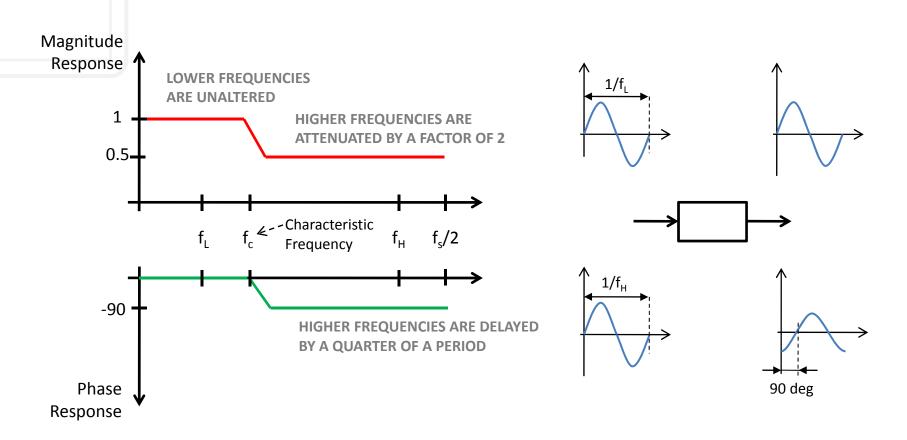


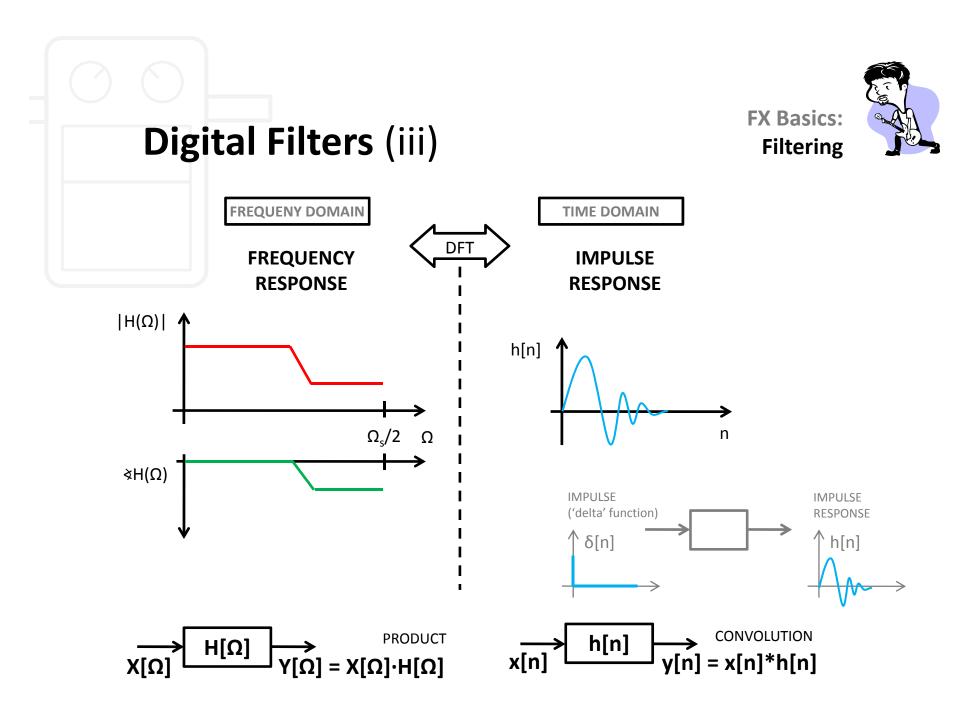
It is common to describe a digital filter in terms of how it affects amplitude and phase of different frequency components of a signal.

Ultimately, the design of digital filters is driven by such desired features. In general, **digital filter design** is not an easy task.



Digital Filters (ii)







Digital Filters (iv)

Digital filters are commonly expressed by their difference equation:

$$y[n] = b_0 \cdot x[n] + b_1 \cdot x[n-1] + ... + b_M \cdot x[n-M] \leftarrow \text{current and previous input samples}$$

$$- a_1 \cdot y[n-1] - ... - a_N \cdot y[n-N] \leftarrow \text{previous output samples}$$

$$= \sum_{i=0}^{M} b_i \cdot x[n-i] - \sum_{j=1}^{N} a_j \cdot y[n-j]$$

$$\longrightarrow \text{NON-RECURSIVE RECURSIVE PART PART}$$

$$\xrightarrow{\text{PART}} b_i \cdot x[n-i] \rightarrow \text{FILTER COEFFICIENTS}$$

$$\xrightarrow{\text{max}(M,N)} \longrightarrow \text{FILTER ORDER}$$

...or by their **transfer function** (in the frequency domain, through the 'Z' transform):

$$H(z) = \frac{Y(z)}{X(z)} = \frac{b_0 + b_1 \cdot z^{-1} + ... + b_N \cdot z^{-M}}{1 + a_1 \cdot z^{-1} + ... + a_N \cdot z^{-N}}$$
 z-M denotes M samples of delay

FX Basics: Filtering

Digital Filters (v)

Two main types of digital filters:

$$H(z) = \frac{b_0 + b_1 \cdot z^{-1} + ... + b_N \cdot z^{-M}}{1 + a_1 \cdot z^{-1} + ... + a_N \cdot z^{-N}}$$

Finite Impulse Response (FIR)

- Presents only b_i coefficients being non-zero : **NON-RECURSIVE**
- Finite h[n]
- Phase response is linear

Infinite Impulse Response (IIR)

- Presents both b_i and a_i coefficients being non-zero: **RECURSIVE**
- Infinite h[n]
- Phase response is non-linear
- Need less computations for similar desired characteristics
- May suffer from numerical problems due to feedback



Digital Filters (vi)

How to explore the frequency domain response of a given filter? Among other options...

SINUSOIDAL ANALYSIS

- Generate a sinusoidal x_i[n] for each frequency f_i to study
- Feed filter with each sinusoidal signal x_i[n] and obtain a sinusoidal y_i[n]
- Obtain magnitude and phase responses for each frequency Ω_i :

$$|H[\Omega_i]| = A(y_i[n])/A(x_i[n]) \qquad \forall H[\Omega_i] = \forall y_i[n] - \forall x_i[n]$$

IMPULSE RESPONSE

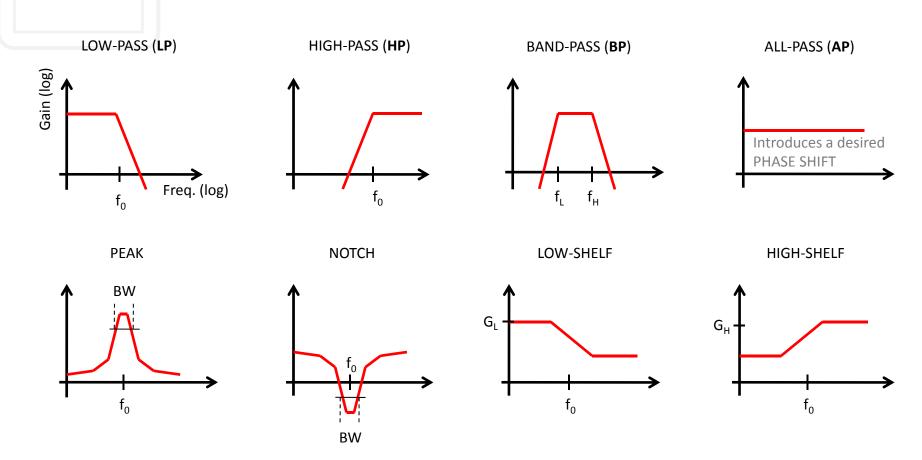
- Generate an impulse 'delta' signal δ[n]
- Feed filter with signal $\delta[n]$ and obtain output signal h[n]
- Obtain H[Ω] via DFT(h[n])
- Obtain magnitude and phase responses as:

$$|H[\Omega]| = abs(H[\Omega])$$
 $\forall H[\Omega] = angle(H[\Omega])$



Digital Filters (vii)

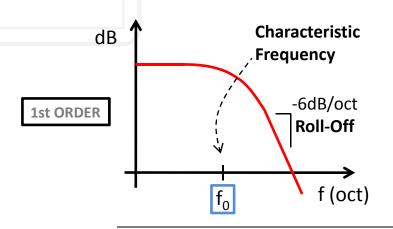
Some **prototypical** basic filters (<u>magnitude</u> response):

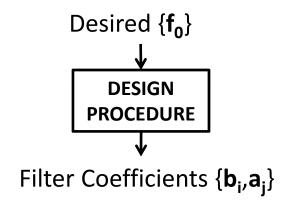


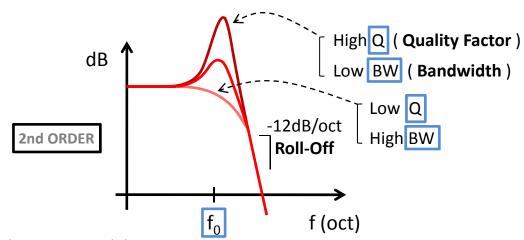


Digital Filters (viii)

LPF (Butterworth) design parameters/constraints:







Desired {f₀,Q} or {f₀,BW}

DESIGN
PROCEDURE

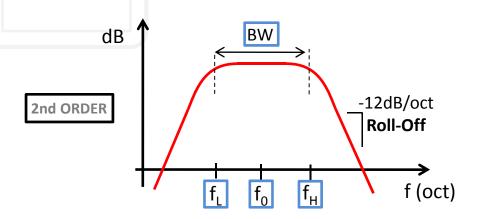
Filter Coefficients $\{b_i, a_j\}$



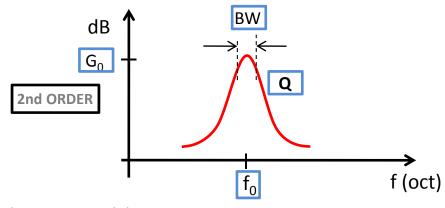


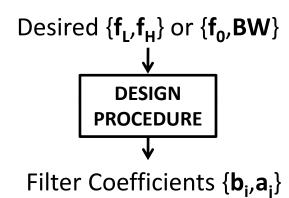
Digital Filters (ix)

BPF design parameters/constraints:



PEAK design parameters/constraints:





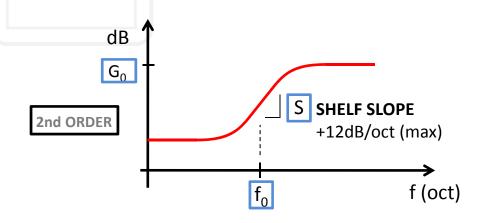
Desired $\{f_0, G_0, BW\}$ or $\{f_0, G_0, Q\}$ DESIGN
PROCEDURE

Filter Coefficients $\{b_i, a_j\}$





HIGH-SHELF design parameters/constraints:



Desired $\{\mathbf{f_0}, \mathbf{G_0}, \mathbf{S}\}\$ **DESIGN PROCEDURE** Filter Coefficients {**b**_i,**a**_i}

All these filters functions can be implemented by means of the 2nd order 'BIQUAD' section:

H(z) =
$$\frac{b_0 + b_1 \cdot z^{-1} + b_2 \cdot z^{-2}}{a_0 + a_1 \cdot z^{-1} + a_N \cdot z^{-2}}$$

How to design them? Extensive theory & literature!!

→ Quick method: R. Bristow-Johnson's cookbook:



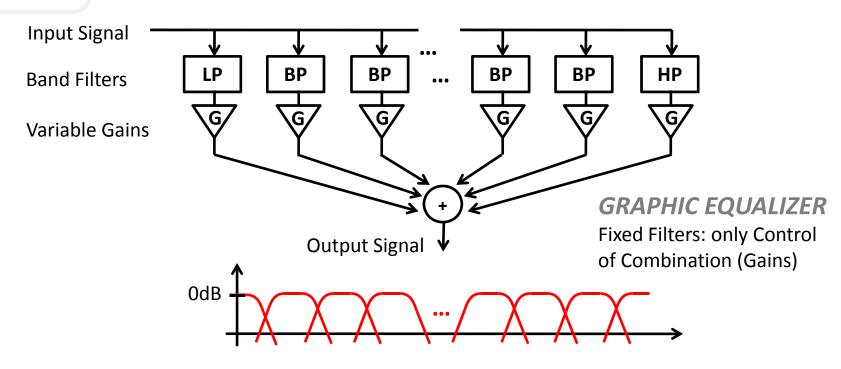
http://www.musicdsp.org/files/Audio-EQ-Cookbook.txt

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Equalization (ii)

N-BAND EQUALIZER by **PARALLEL** BAND-DEDICATED, FIXED FILTERS

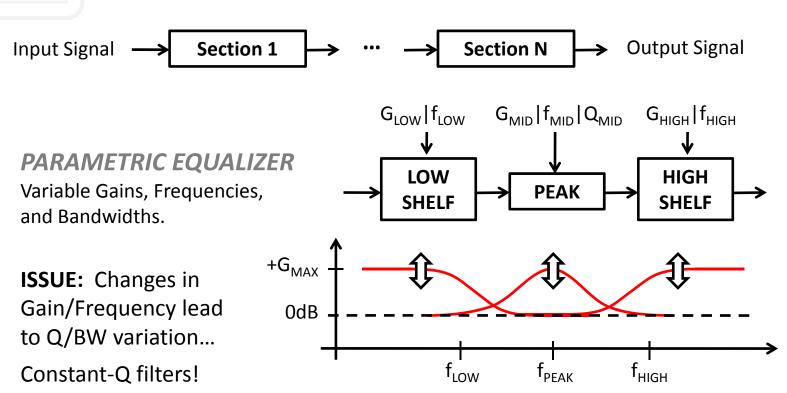


ISSUE: Phase shifts introduced by different IIR filters may cause undesired effects when summing overlapping bands... Compensate with ALL-PASS filters?



Equalization (iii)

N-BAND EQUALIZER by **CASCADE** of BAND-DEDICATED, CONTROLLABLE SECTIONS





http://www.rane.com/note101.html



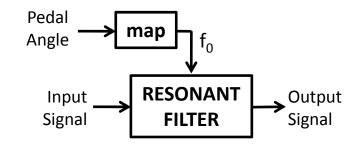
Wah-wah

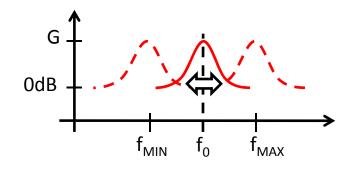
Dating back from the 60s, its name was given after voice tone modulation (formant shift) caused by transition between vowels.

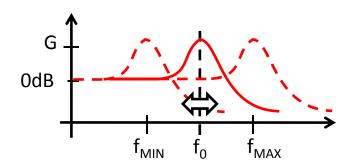


http://www.geofex.com/article_folders/wahpedl/voicewah.htm

In its most basic form, it consists on shifting the center frequency of a resonant filter (Peak BP or LP)







pd~

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