Search-Effectiveness Measures for Symbolic Music Queries in Very Large Databases

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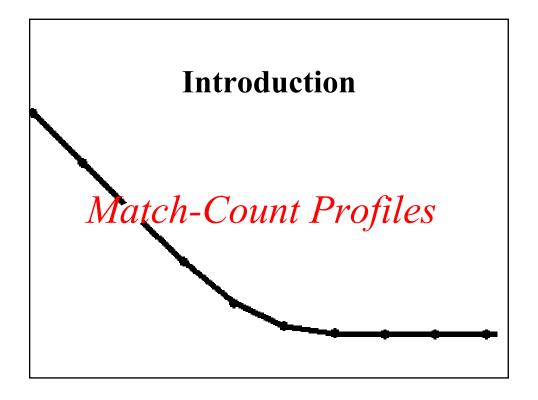
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Musical Features

• We examined search characteristics of 14 musical features:

7 Pitch features (examples below)

7 Rhythm features: (3 duration & 4 metric)

- 4. beat level (2)
- 1. duration (37~74)
- **5**. metric level (10~14)
- 2. duration gross contour (3)
- **6**. metric gross contour (3)
- 3. duration refined contour (5)
- 7. metric refined contour (5)



• How do all these different features affect searching in a database?

Anchored vs. Unanchored Searches

Search Pattern: F A C

Two types of search methods, Examples:

Anchored Matches search only from the start of a database entries



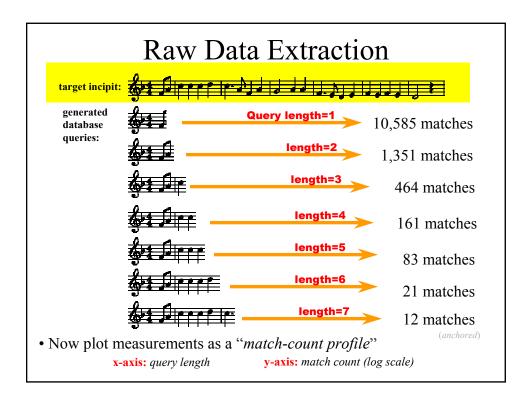
Unanchored Matches search starting at any position in database entries

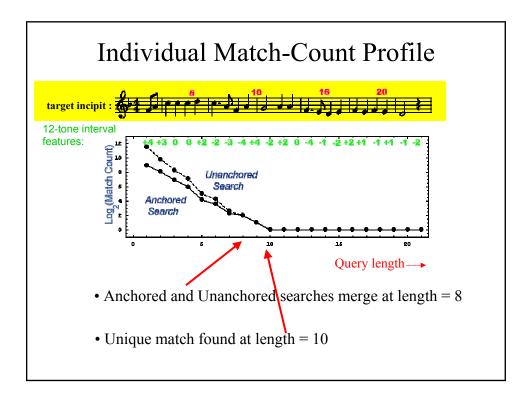


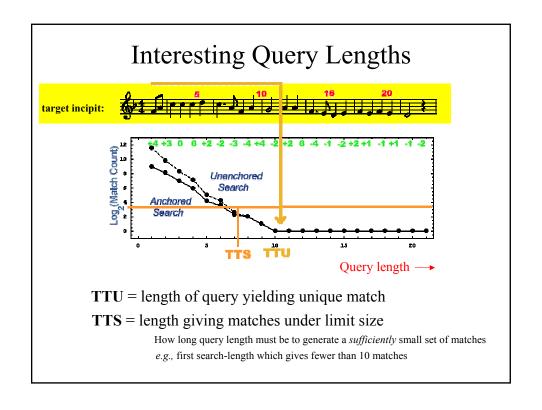
Example Feature Searches

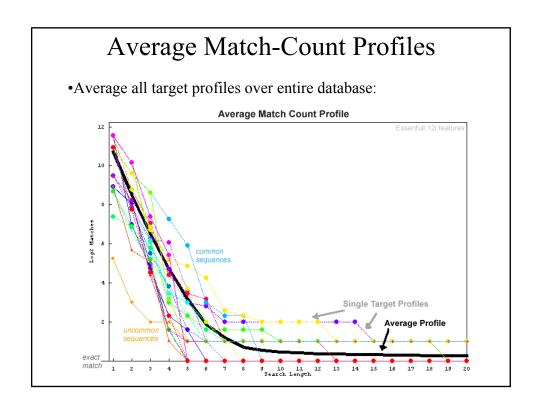


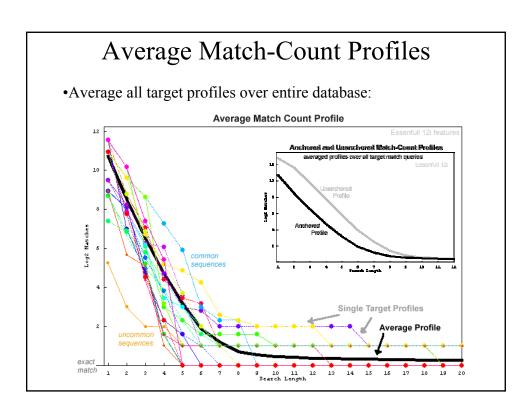
| | Feature | Query (in Themefinder) | Anchored Matches | Unanchored Matches |
|-----------------------|---------|------------------------|------------------------|-----------------------------|
| pitch name | pch | F A C | 464 | 1,710 |
| 12-tone pitch | 12p | 5 9 0 | 464 | 1,710 |
| musical interval | mi | +M3 +m3 | 1,924 | 6,882 |
| 12-tone interval | 12i | +4 +3 | 1,925 | 6,894 |
| scale degree | sd | 1 3 5 | 2,009 | 7,024 |
| pitch refined contour | prc | UU | 4,677 | 17,712 |
| pitch gross contour | pgc | UU | 19,787 | 76,865 |
| | | Searchir | ng a database of 100.0 | 000 melodic incipits/themes |

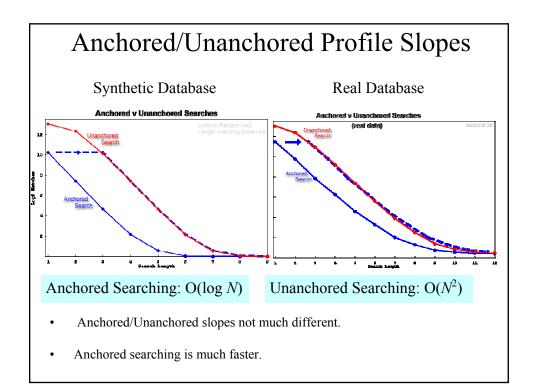


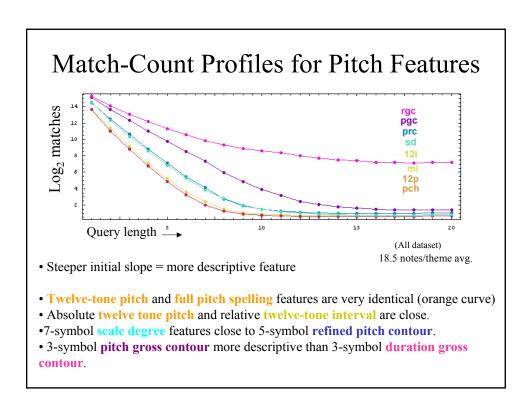




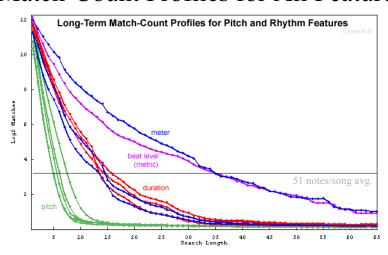








Match-Count Profiles for All Features



- TTS for rhythm twice as long than pitch TTS.
- TTS for gross metric descriptions 5 times as long as pitch TTS values.
- Rhythm feature curves more crooked.

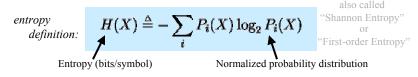
 Phrase/meter effects?

Four Applications of Profiles:

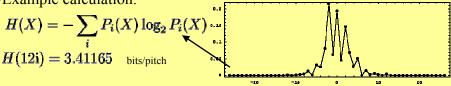
- Entropy & Entropy Rate
- Joint Feature Analysis
- Match Count Predictions
- Synthetic Database Analysis

Entropy

• Entropy measures basic information content of a musical feature



•Example calculation:

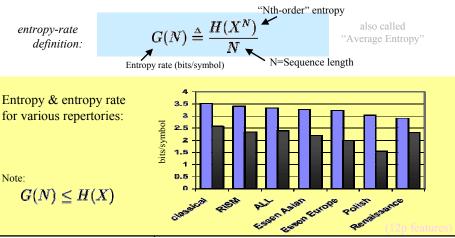


12-tone interval distribution

➤ 3.4 bits/note is the minimum symbol storage size needed to store sequences of 12-tone intervals (Folksong data set).

Entropy Rate

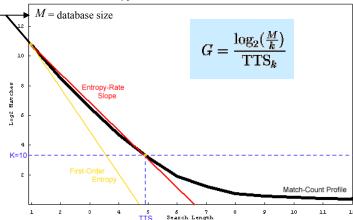
- Entropy is a contextless (memoryless) measure.
- Real music features are related to surrounding musical context.
- Average entropy (entropy-rate) is more informative:



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Entropy-Rate Estimation from TTS





- Entropy characterizes the minimum possible average TTS.
- Entropy-rate characterizes the actual average TTS.

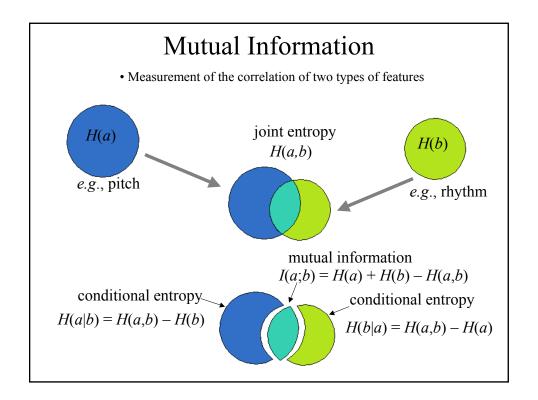
• Entropy & Entropy Rate

- Joint Feature Analysis
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Joint Feature Analysis

Analyze
Pitch + Rhythm
as a combined feature

- How independent/dependent are pitch and rhythm features?
- What is the effect of searching pitch and rhythm features in parallel?



Combining Pitch and Rhythm Searches



Individual Entropies:

$$H(pgc) = 1.5325$$

$$H(rgc) = 1.4643$$

Joint Entropy:

$$H(pgc, rgc) = 2.9900$$

Mutual Information:

$$I(\mathbf{pgc}; \mathbf{rgc}) = H(\mathbf{pgc}) + H(\mathbf{rgc}) - H(\mathbf{pgc}, \mathbf{rgc}) = 0.0068$$

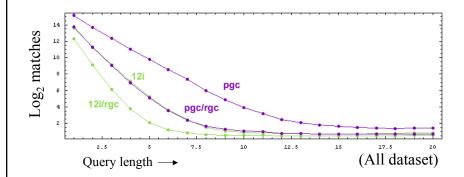
less than two orders of magnitude interaction

- Pitch and Rhythm are very independent features.

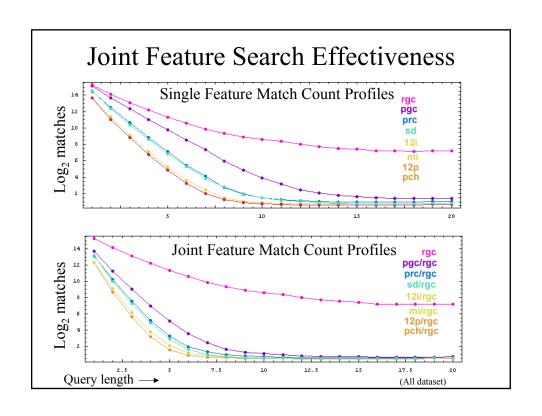
 (at least for pgc+rgc averaged over entire database)
- Therefore, combining independent search features should be effective.

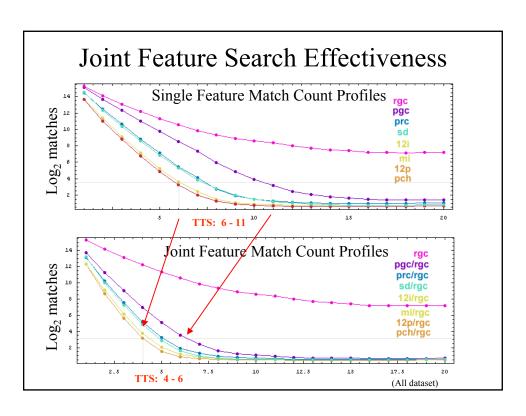
Joint Feature Profiles

for pgc/rgc vs. twelve-tone interval searching



- 3*3 states work as well as 88 twelve-tone interval states.
- pgc and rgc are generic features less prone to query errors.





- Entropy & Entropy Rate
- Joint Feature Analysis
- Match Count Predictions Synthetic Database Analysis

Expectation Function

• Entropy Rate can be used to predict the number of matches:

$$E(n) = \frac{M}{R^n}$$
 database size $R = 2^H$ (H = measured entropy rate)

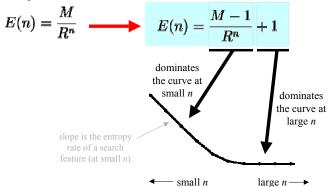
Expected match counts for an n-length query

- Example:
 - Consider a database of "best 3 out of 5" Heads/Tails coin flips:

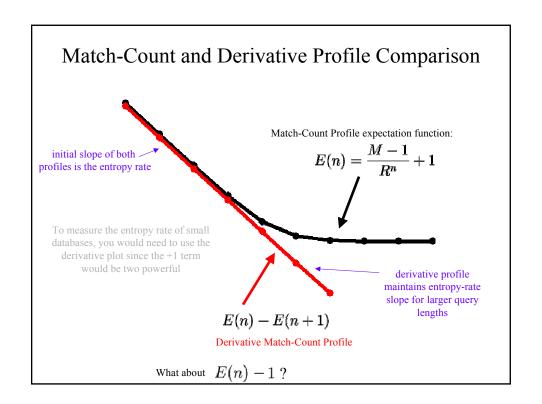
- Likelyhood starting sequence is "H": 50%
- $E(1) = M/2^1 = M/2$
- Likelyhood starting sequence is "H T": 25%
- $E(2) = M/2^2 = M/4$
- Likelyhood starting sequence is "H H": 25%
- $E(2) = M/2^2 = M/4$

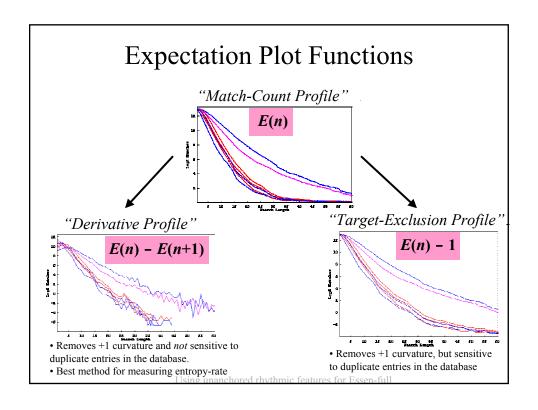
Match-Count Profile Constraint

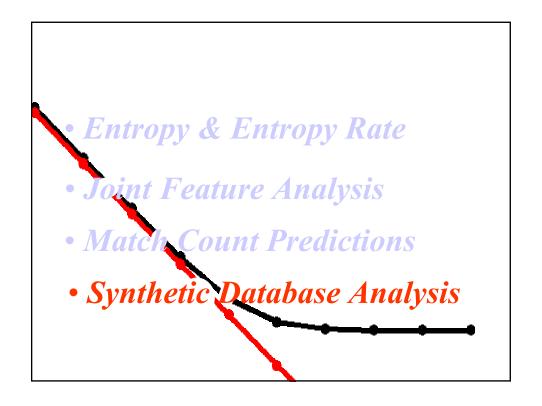
- The match-count profile queries are constructed from database entries.
- Therefore at least one match is always expected.
- Steal this guaranteed match from M, and add as a constant to the expectation function:

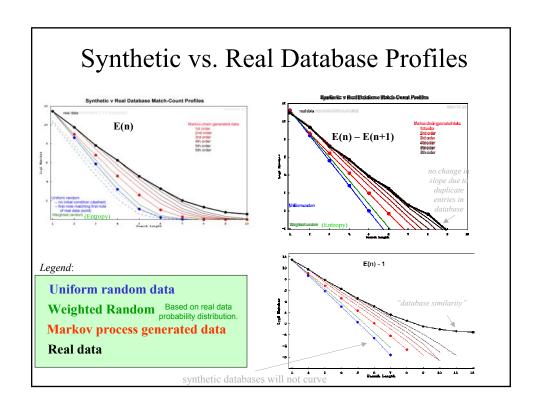


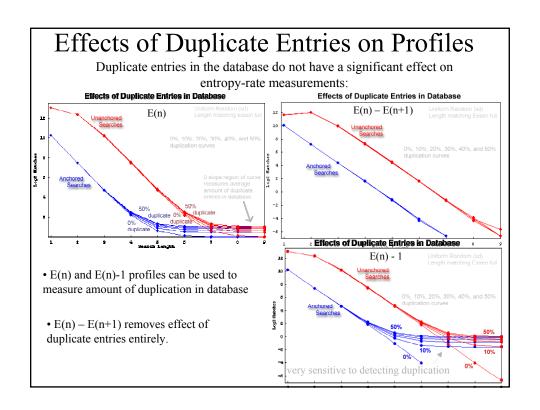
• How to get rid of curvature caused by constant +1 term?

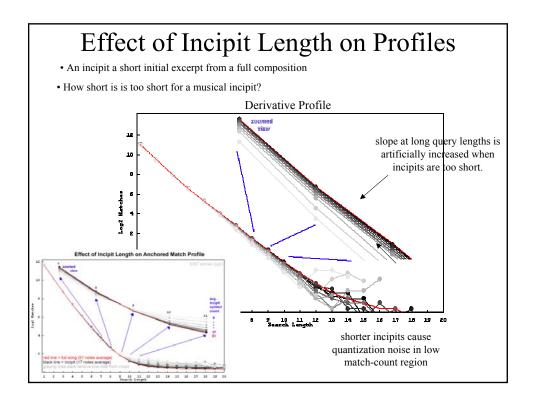












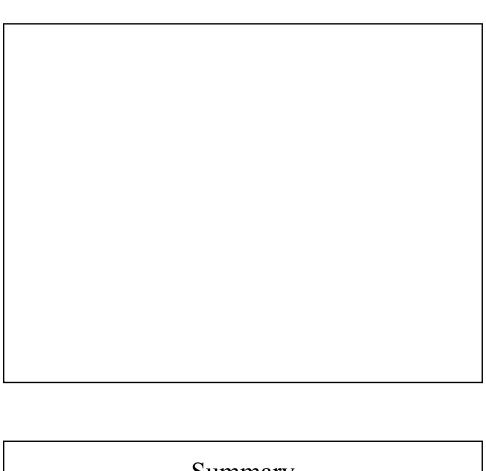
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Summary

Interesting metrics for analyzing the effectiveness of search features:

- •Match-Count Profiles: Examines match characteristics of a musical feature for longer and longer queries.
- •Entropy Rate: Characterizes match count profiles well with a single number. Useful for predicting the expected average number of matches for a given length query.
- •**TTS:** The number of symbols in query necessary to generate a sufficiently small number of matches (average). TTU not as useful due to noise.

Proof for Derivative Plots

$$E(n) = rac{M-1}{R^n} + 1$$
 (expectation function for Match-Count Profiles)

$$E(n)-E(n+1)=rac{M-1}{R^n}-rac{M-1}{R^{n+1}}$$
 (subtract n and $n+1$ values of $E(n)$ to cancel $n+1$ term)

$$E(n) - E(n+1) = \frac{(R-1)(M-1)}{R R^n}$$
 (algebra manipulation) plotting on a log scale, so take the log of both sides:

$$\log_2[E(n) - E(n+1)] = \log_2\left[\frac{(R-1)(M-1)}{R}\right] - \log_2 R^n$$

Let:
$$y = \log_2[E(n) - E(n+1)]$$
 and $b = \log_2\left[\frac{(R-1)(M-1)}{R}\right]$ so the equation becomes: $y = b - \log_2 R^n$

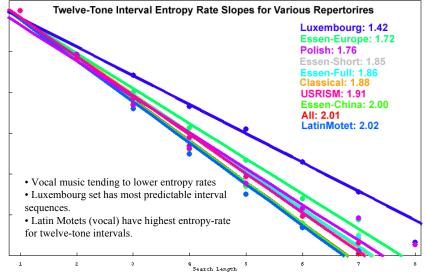
$$y = b - \log_2 2^{Hn}$$
 since $R = 2^H$

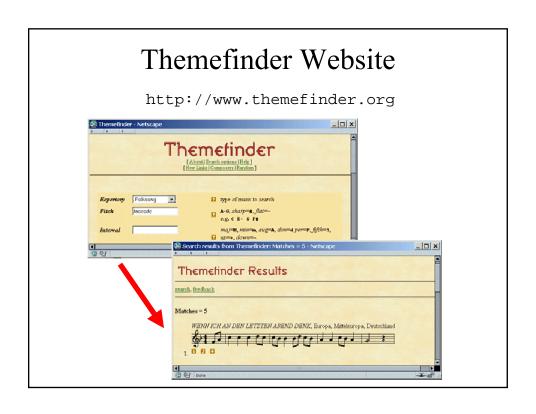
Let: x=n

$$y = -Hx + b$$

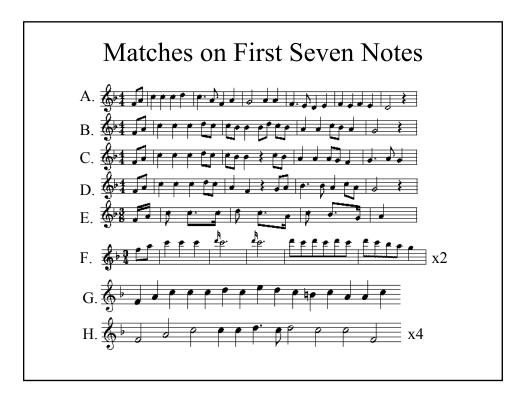
which is a line with a slope proportional to the entropy (rate)

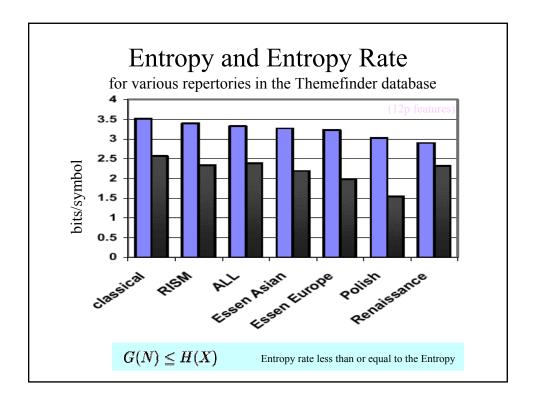
Derivative Plots for 12i features

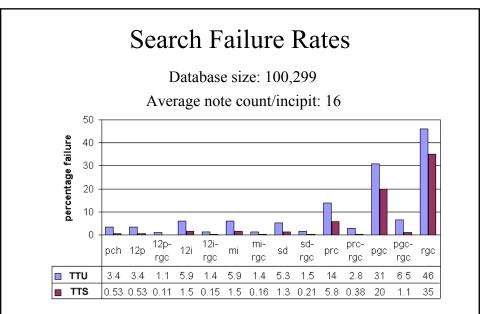




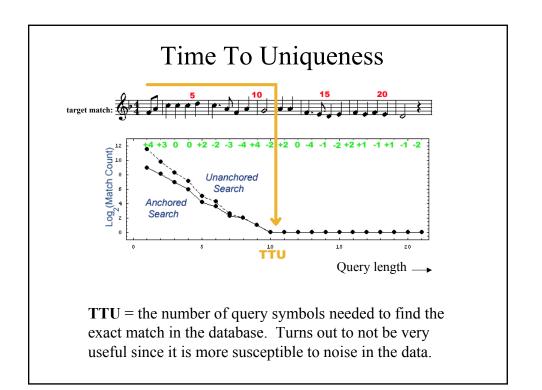
| Themefinder Collections | | | | | |
|-------------------------|-----------------|-------------------------------|--|--|--|
| Data set | Count | Web Interface themefinder.org | | | |
| Classical Folksong | 10,718 8,473 | themefinder.org | | | |
| Renaissance | 18,946 | latinmotet.themefinder.org | | | |
| US RISM A/II | 55,490 | | | | |
| Polish | 6,060 | | | | |
| Luxembourg | 612 | lux.themefinder.org | | | |
| total: | 100,299 | | | | |

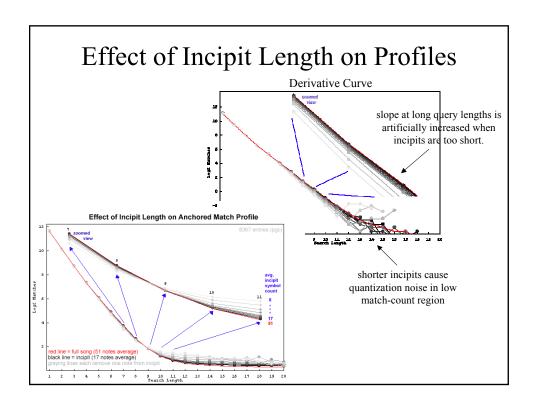


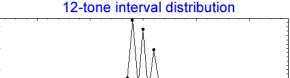




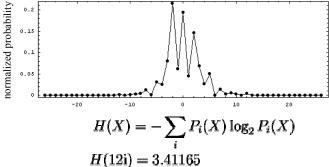
•Plot measures how often a search produces too many matches for query sequences as long as the database entry.







Probability Distributions



- 3.4 bits/note is the lower symbol storage size limit needed to store sequences of 12-tone intervals (Folksong data set).
- Entropy can be used as a basic estimate for how many notes are necessary to find a unique/sufficient match in the database, but ...

Expectation Function

$$M$$
 = database size

$$E(n)$$
 = average expected match counts for an *n*-length query

$$R=2^{H}$$
 where H is the entropy rate of the feature being searched for (Entropy rate is assumed to be constant)

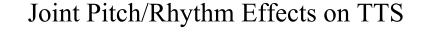
In general:
$$E(n)=rac{M}{R^n}$$

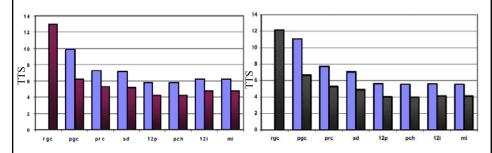
For example, consider sequences created with a uniform random distribution of three states (the next symbol in the sequence is equally likely to be any of the three states).

Then, the entropy of the sequence is:
$$H = \log_2 3$$
 which makes $R = 2^{\log_2 3} = 3$

and the formula for the expected match counts becomes:
$$E(n)=rac{M}{3^n}$$

then 1/3 of the database entries should be matched with a one-
$$E(1)=\frac{M}{3^1}=\frac{M}{3}$$
 and a length-two query should return 1/9 of the $E(2)=\frac{M}{3^2}=\frac{M}{9}$ length query on the average:





Chinese Folksongs dataset

Classical dataset

- •Adding rgc to pitch features usually reduces the search length by 2 notes.
- •Combining rgc and pgc reduces search length by 4 notes.